# DETERMINATION OF THE PARAMETERS OF THE DEFAULT ISOMETRIC VIEW USING METHOD OF RECTANGULAR AUXILIARY PROJECTION 

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#### Abstract

This article describes the definition of the parameters of standard isometry using the model of rectangular auxiliary projection in a graphical way. Also improved projection apparatus of this method, so that the Z axis was in a vertical position.


Keyword: Transformations, graph, isometric, options, a diagonal of a cube orthographic projection, pictorial representation, an imaginary plane, projecting the beam, the carrier of the projection, the distortion coefficient.

## INTRODUCTION, LITERATURE REVIEW AND DISCUSSION

This article describes the definition of distortion coefficients on axonometric axes $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ and angles between them of standard isometry using the transformation model-diagram of the method of rectangular auxiliary projection.

The founder of this method is a well-known Ukrainian scientist on descriptive geometry, doctor of technical Sciences Professor S. M. Kolotov [1]. The essence and content of the rectangular auxiliary projection method is as follows:

Geometric images on the Monge plot are projected on a parallel or perpendicular plane, so that these images are simultaneously projected without distortion on them and on the frontal plane of projections.

For rice. 1 shows the determination of the length of a horizontally projecting straight line AB , length 100 mm , on the plane $\mathrm{P}\left(\mathrm{P}_{\mathrm{H}} \mathrm{Pv}\right)$, which is depicted by thin lines, the method of rectangular projection.

For this purpose the Kolotov diagram is constructed - the device of rectangular auxiliary projection for construction of isometric projections.

Which consists of a plane $P$, the traces of which are located at an angle of $45^{\circ}$ to the axis of projection, and the direction of projection s (s's") perpendicular to it. Because in isometry, the projection direction is parallel to the diagonal of the cube.

With this direction s , the horizontal segment AB lying simultaneously on the plane P and H , is projected onto the plane $V$ without distortion in full size $A^{\prime} B^{\prime}=A^{\prime \prime} B_{0}$. In this case, the point in $\mathrm{B}_{0}$ is obtained as a result of the intersection of the arc radius $\mathrm{A}^{\prime} \mathrm{B}^{\prime}$ and the center $\mathrm{A}^{\prime} \mathrm{c}$ with the front projection s " of the projection direction s .

Through the point $B_{0}$ conducting a straight line perpendicular to $к$ $A$ " $B_{0}$ we get the direction
of the projection carrier. Thus for construction of a new projection of characteristic points of objects, it is enough to find a point of intersection of each direction of the carrier of a projection of points with a line passing through them in parallel s", i.e. similarly as a point $\mathrm{B}_{0}$.


Fig. 1
From the picture it can be seen that the projection carrier of this device is a reflection of the rays coinciding with the horizontal projection of the projection direction s'. Where the plane of reflection is the bisector plane of the angle $\mathrm{B}^{\prime} \mathrm{A}^{\prime} \mathrm{B}$. In this case, the point $\mathrm{B}_{0}$ can also be obtained by crossing the reflecting beam $\mathrm{s}^{\prime}$ at the point $\mathrm{B}_{\bar{\sigma}}$ lying on the bisector plane of the projection apparatus.

Thus, the elements of the apparatus of rectangular auxiliary projection of isometric projections are:

1. The projection direction $\mathrm{s}\left(\mathrm{s}^{\prime} \mathrm{s}\right.$ ") and the imaginary projection plane p perpendicular to it;
2. The bisector plane line drawn between the imaginary plane and the projection plane V;
3. A projection medium is a projection of a geometric object.

With the help of these elements of the projection apparatus we proceed to the solution of the above task:

1. Through the points $\mathrm{A}^{\prime \prime}$ and $\mathrm{B} "$ we draw parallel lines to $\mathrm{s}^{\prime \prime}$, i.e. the segment of the straight line $A B$ is projected onto the plane $P$ perpendicular to the direction $s$ :
$\mathrm{s}^{\prime} \perp \mathrm{P}_{\mathrm{H}}$ and $\mathrm{s} " \perp \mathrm{P}_{\mathrm{V}}$;
Through the points $A^{\prime} \equiv \mathrm{B}^{\prime}$ we draw a line that is parallel to $\mathrm{s}^{\prime}$, as the incident line projecting to the trace of the bisector plane and reflecting from it the projection carrier;
2. New projections Ao and Bo points A and B are obtained as points of intersection of the projection carrier with parallel lines passing through points $A^{\prime \prime}$ and $B^{\prime \prime}$. Connecting the obtained points, we construct an isometric projection a AoBo the straight line AB.

If we imagine a horizontally projecting straight line $A B$ as the $Z$ axis of the Cartesian coordinate system, then the distortion of the straight line AB will be the distortion of the axis equal to $81,65 \mathrm{~mm}$.

It is known that in the method of auxiliary projection geometric images are depicted as a visual, i.e. axonometric projection. In this case, the Z axis and the faces parallel to it in the isometry are inclined $15^{0}$ from the vertical to the right.

Having creatively analyzed these properties of the isometry constructed by the method of rectangular auxiliary projection, so that $T h e \mathrm{Z}$ axis turned out to be vertical, we decided to turn the isometry projection apparatus $15^{0}$ to the left, i.e. counterclockwise. Where the center of rotation is taken point $\mathrm{A}^{\prime} \equiv \mathrm{A}^{\prime \prime}=\mathrm{P} \mathrm{V} \cap \mathrm{OX}$ (axis of projections).
In this case, the elements of the isometric projection apparatus occupy the position as fig. 2:

- the $\mathrm{P}_{\mathrm{H}}$ angle with the axis of projection of $30^{\circ}$;
- $\mathrm{P}_{\mathrm{V}}$ angle with $60^{\circ}$ projection axis;
- horizontal projection angle of projection direction s' with projection axis $60^{\circ}$;
- the angle of the front projection of the projection direction s " with a projection axis of $30^{\circ}$;
- track angle of the bisector plane with a projection axis of $15^{\circ}$;
- the angle of direction of the new projection carrier with the projection axis of $90^{\circ}$, i.e. perpendicular to the projection axis of the $\mathrm{H} / \mathrm{V}$ system.

For rice. 3 shows the sequence of projection of the horizontal straight line $A B$ on the plane P , which is perpendicular to the direction of projection $\mathrm{s}\left(\mathrm{s}^{\prime} \mathrm{s}\right.$ "):


Fig. 2


Fig. 3

1. Draw as in Fig. 3 the left elements of the projection apparatus to rotate by $15^{\circ}$ and

2. In the direction $s$ "we project the ends of the segment on the plane P and get the points $\mathrm{A}_{2}$ ", $\mathrm{B}_{2}$ and transfer them to the plane $\mathrm{P}_{1}$;
3. Through these points, which lie on $\mathrm{P}_{1 \mathrm{v}}$, we draw parallel lines to $\mathrm{s}_{1}$ " and to the right we build a trace of the bisector plane of the projection apparatus so that the new projection of the line segment AoBo is built to the side;
4. And thus from the point $\mathrm{A}_{2} \mathbf{B}_{2}{ }^{\prime}$ (it can be arbitrarily taken on $\mathrm{P}_{1 \mathrm{H}}$ ) we draw a line that is parallel to s 1 ' to the intersection with the trace of the bisector plane, as an incident ray.

We conduct a reflecting beam - carrier projection, which intersecting with parallel lines drawn through the points $\mathrm{A}_{2}$ " and $\mathrm{B}_{2} "$ will give the points Ao and Bo. Combining them we obtain a projection of a segment of a horizontally projecting straight line $A B$, as the $Z$ axis of the Cartesian coordinate system.

Thus, improving the apparatus of the method of parallel auxiliary projection, It is possible to obtain the Z axis and parallel faces of geometric images vertically.

Using this improved apparatus in Fig. 4 and 5 the cube isometry and axonometric projections


Fig. 4
Fig. 5
The French engineer Frezier at the time of the birth of the course of descriptive geometry Gaspard Monge, and more than a century and a half later scientists Kolotov and Gordon, as well as scientists India Rana and Shah established that the orthogonal isometric projection of the cube is a regular hexagon, as in Fig. 4.

Thus, as a result of our research, we showed the possibility of graphical determination of the parameters of standard isometry using the method of rectangular auxiliary projection, i.e. distortion coefficients along the $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ axes equal to the theoretical 0.816496 . And the angle between them is $120^{\circ}$.

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