SOME CRITERIA FOR PLURIHARMONICITY

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ABSTRACT

In this article we prove an analogue of Hartogs' Lemma for pluriharmonic functions:

Theorem I. Suppose that the function $U(z, z_n)$ is defined in polydisk ${}^{\prime}V \times \{|z_n| < R\} \subset C_{z_n}^{n-1} \times C_{z_n}, R > 0$ and satisfies the following conditions:

1) For each fixed $z \in V$ function $U(z, z_n)$ of a complex variable z_n harmonic in the circle $|z_n| < R$

2) U('z,0) is harmonic in 'V on 'z

3) function $U(z, z_n)$ is plurisubharmonic in all variables in some polydisk $V \times \{|z_n| < r\}, R > r > 0$

Then, the function $U(z, z_n)$ is pluriharmonic in polydisk $V \times \{ |z_n| < R \}$

Keywords: Hartogs' Theorem, Lelong's theorem, separately holomorphic functions, separately harmonic functions, holomorphic functions, harmonic functions, plurisubharmonic functions.